**Barron’s Let’s Review Regents – Algebra II**

# Chapter 10: Standard Deviation

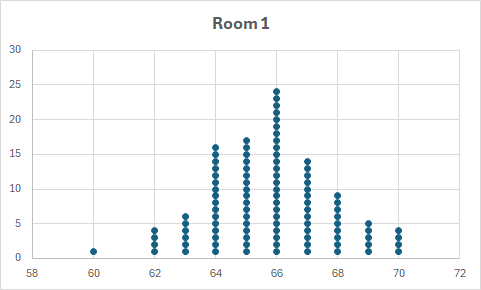
## 10.1 Standard Deviation

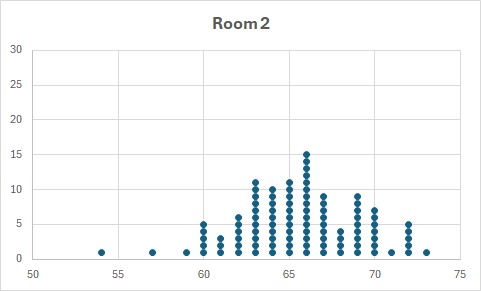
**Key Ideas**

The *standard deviation* of a set of numbers is a measure of how “spread out” the numbers in a set are. The more spread out the numbers are, the larger the standard deviation.

**Comparing Standard Deviations for Two Data Sets with the Same Mean**

Two rooms each have 100 people in them. The mean (average) height of the people in each room is approximately 66 inches. Even though the rooms have the same number of people and the same mean, there is something very different about the collection of people in each room. Below are the dot plots for room 1 and room 2.





The people in room 1 are mostly very close to the 66-inch average. There are people in room 2, though, who are much shorter than the average and people who are much taller than the average.

In statistics, we say that the set of people in the second room have a higher standard deviation. The standard deviation for the heights of the people in the room 1 was approximately 2, while the standard deviation for the heights of the people in room 2 was 6.

**Example 1**

Each of the dot plots below has a mean of approximately 40. Which of the dot plots below corresponds to the set with the lowest standard

**Calculating Standard Deviation with Microsoft Excel**

Excel has built-in functions like AVERAGE for the mean and STDEV.S (for sample standard deviation) or STDEV.P (for population standard deviation) to calculate these values directly.

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**Calculating Standard Deviation with Microsoft Edge Add-ons**

[Standard Deviation Calculator](https://microsoftedge.microsoft.com/addons/detail/standard-deviation-calcul/cgobbibhehfoedopeahebikmmdkahlfc?hl=en-US)

**Calculating Standard Deviation with Omni Calculator**

[Omni Calculator](https://www.omnicalculator.com/statistics/z-score), which can calculate both mean and standard deviation.

**Calculating Mean and Standard Deviation with Geogebra**

[One Variable Stats on Geogebra](https://www.youtube.com/watch?v=jcXKwU3O6Po)

1. Use Geogebra Classic.
2. Select Spreadsheet view.

A screenshot of a graphing application

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1. Copy data from Spreadsheet column into Geogreba Spreadsheet column(s). Delete the first row if it contains a header (necessary?)

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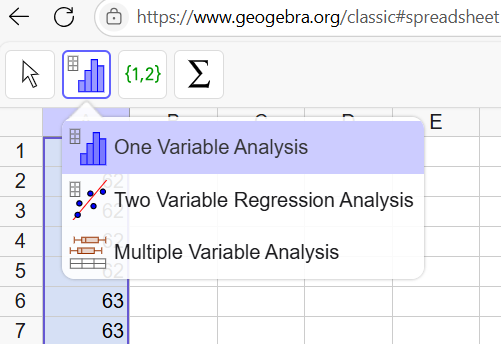
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1. Click One Variable Analysis tool.

A yellow and blue bar graph

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1. Select One Variable Analysis menu button.



1. A histogram is displayed. Click the button.

A graph on a computer screen

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The mean and standard deviation is displayed.

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**Standard Deviation for Sets with Repeated Numbers**

Entering all the numbers for a large data set into the calculator can be very time consuming. If however, there are many repeated numbers, you can use a shortcut. Below the data for 55 numbers are summarized in a *frequency table*. The 7 in the frequency column after the number 42 means that there are seven 42s in the data set.

|  |  |
| --- | --- |
| **Number** | **Frequency** |
| 42 | 7 |
| 53 | 9 |
| 61 | 12 |
| 74 | 8 |
| 86 | 4 |
| 127 | 10 |
| 150 | 5 |

**Using Microsoft Excel to Create Histogram Using Frequency Table**

1. Select the table in Excel

A screenshot of a spreadsheet

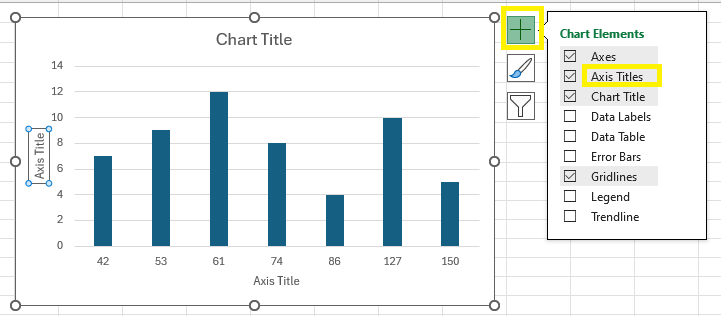
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1. On Insert Tab, select Recommended Charts. Select Clustered charts.

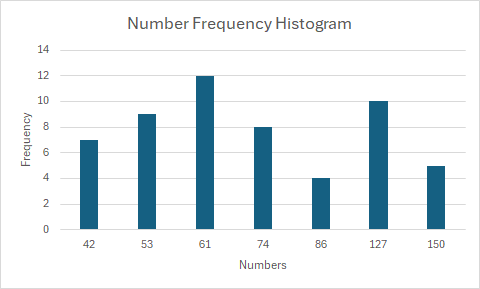
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1. Select + button followed by clicking checkbox for Axis Titles. Horizontal and Vertical axis title regions appear.



1. Type in Numbers for Horizontal axis title and Frequency for Vertical axis title. Change the Chart Title to Number Frequency or Number Histogram.



**Using** [**GeoGebra Calculator Classic**](https://www.geogebra.org/classic)

1. Click on above link for GeoGebra Calculator Classic.
2. Click Spreadsheet option. Refresh browser page if this does not appear.

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1. Copy and paste table data from Word, Excel or Comma Separated Value file using Hamburger menu bar. If opening Command

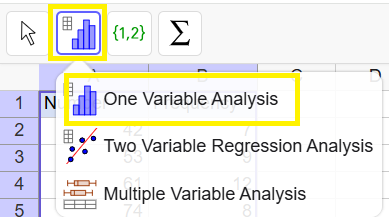
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1. Select both columns. Click Histogram button. Click One Variable Analysis

A screenshot of a table

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1. Select Bar Chart.

A screenshot of a graph

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1. Clicking on the bar chart displays some display options, such as setting the bar width.

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1. Statistics can be displayed by clicking the Sigma x button.



The mean, population standard deviation , sample standard deviation, minimum, maximum, median and quartiles are displayed, among other items.

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**z-scores**

In a data set with a mean of 60 and a standard deviation of 4, the number 64 is one standard deviation above the mean since it is equal to the mean plus the standard deviation. The number 68 is two standard deviations above the mean since it is equal to the mean plus two times the standard deviation .

In statistics, we say that a number that is one standard deviation above the mean has a *z-score* of 1, while a number that is two standard deviations above the mean has a z-score of 2.

**Math Facts**

The *z-score* of a number is how many standard deviations above or below the mean that number is. If the number is greater than the mean, the z-score is positive. If the number is less than the mean, the z-score is negative.

A formula for calculating z-score is   
.

**Example 3**

If the mean is 60 and the standard deviation is 4, what is the -score of the number 52?

*Solution*: Since 52 is less than 60, the -score will be negative. For this example, it is possible to subtract the standard deviation, 4, from 60 to get to 56, which has a -score of -1. Then subtract it again to get to 52, which has a -score of -2.

This can also be calculated with the formula   
.

**Example 4**

If the mean is 40 and the standard deviation is 7, what is the -score of the number 50?

*Solution*: The -score must be between 1 and 2, since while would have a -score of 2.

Use the formula:

**Example 5**

If the mean is 73 and the standard deviation is 8, what number has a -score of -1.5?

*Solution*: Multiple the -score by the standard deviation to get . Add this to the mean to get , which is the number that has a -score of -1.5.

This can also be done with the formula with as a known variable and the number is unknown.

### Check Your Understanding of Section 10.1

1. *Multiple-Choice*
2. Each of these data sets has a mean of 5. Which has the smallest standard deviation?

**(3) 4, 5, 5, 5, 6**

1. What is the standard deviation of the data set 16, 19, 14, 12, 10, 15, 15, 16  
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   **(1) 2.5**
2. What is the standard deviation for this data set?

|  |  |
| --- | --- |
|  |  |
| 18 | 4 |
| 19 | 7 |
| 20 | 2 |
| 21 | 3 |
| 22 | 6 |

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**(2) 1.51**

1. If the mean of a data set is 60 and the standard deviation is 8, what is the z-score for the number 72?  
   **(4) 1.50**
2. If the mean of a data set is 40 and the standard deviation is 6, what number has a -score of -2.5?  
   **(1) 25**
3. Which number has a -score closest to -1 in in the data set 45, 38, 47, 41, 42, 34, 46, 37?  
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   **(4) 37**
4. If the mean of the data set is 41 and the standard deviation is 6, which of the following has a -score between 1.5 and 2.0?  
   **(4) 51**
5. How many of these 8 numbers are more than two standard deviations from the mean?

18, 40, 44, 45, 48, 50, 50, 68  
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18 is the only number more than 2 standard deviations away.  
**(1) 1**

1. How many of these 8 numbers are more than two standard deviations from the mean?

11, 49, 52, 52, 53, 53, 55, 90  
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11 more than 2 std dev

**(1) 1**

1. What percent of these 14 numbers have a -score between -1 and +1?

59, 62, 54, 58, 62, 62, 55, 56, 65, 64, 58, 53, 59, 61

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Outside of range: 54, 55, 65, 64  
Inside range:

**(2) 71%**